## Algebra 2

Section 3.1
Solving Linear Systems by Graphing
system of equations: A set of two or more equations.

$$
\text { Example: } \begin{aligned}
-3 x+2 y & =8 \\
x+2 y & =-8
\end{aligned}
$$

linear system: consists of linear equations \{form a straight line, when graphed\}
solution of a system: A set of values for the variables that makes all equations, in the system, true. The point at which the lines intersect.

What is the solution of the system?

$$
\begin{gathered}
-3 x+2 y=8 \\
x+2 y=-8
\end{gathered}
$$

Graph each equation by getting into slope-intercept form, $\mathbf{y}=\mathrm{mx}+\mathrm{b}$ m is the slope
$\mathbf{b}$ is the $\mathbf{y}$-intercept

$$
\begin{aligned}
& x+2 y=-8 \quad\{\text { second equation }\} \\
& -x \quad-x \\
& 2 y=-x-8 \quad \text { \{subtracted } x \text { from each side }\} \\
& \left.y=-\frac{1}{2} x-4 \quad \text { \{divided each side by } 2\right\} \\
& \text { slope }=-\frac{1}{2} \\
& y \text {-intercept }=-4
\end{aligned}
$$

$$
-3 x+2 y=8 \quad\{\text { first equation }\}
$$

$$
+3 x \quad+3 x
$$

$$
2 y=3 x+8 \quad \text { \{added } 3 x \text { to each side }\}
$$

$$
y=\frac{3}{2} x+4 \quad\{\text { divided each side by } 2\}
$$

$$
\text { slope }=\frac{3}{2}
$$

$$
y \text {-intercept }=4
$$

## check in each equation

$$
\begin{array}{ll}
-3 x+2 y=8 & x+2 y=-8 \\
-3(-4)+2(-2)=8 & -4+2(-2)=-8 \\
12-4=8 & -4-4=-8 \\
8=8 \\
\hline & -8=-8
\end{array}
$$


$(-4,-2)$ is the solution of the system

Find the point of intersection of the two lines:

$$
\begin{aligned}
& 2 x+4 y=12 \\
& x+y=2
\end{aligned}
$$

$$
\begin{aligned}
& x+y=2 \quad \text { \{second equation }\} \\
& -x \quad-x
\end{aligned}
$$

$$
y=-x+2 \quad\{\text { subtracted } x \text { from each side }\}
$$

Graph each equation by getting into slope-intercept form, $y=m x+b$ m is the slope
slope $=-1$
$y$-intercept $=2$
$\mathbf{b}$ is the $\mathbf{y}$-intercept

$$
\begin{aligned}
& \begin{array}{l}
2 x+4 y=12 \\
-2 x \quad-2 x
\end{array} \quad\{\text { first equation }\} \\
& 4 y=-2 x+12 \quad\{\text { subtracted } 2 x \text { from each side }\} \\
& y=-\frac{1}{2} x+3 \quad\{\text { divided each side by } 4\}
\end{aligned}
$$

$$
\text { slope }=-\frac{1}{2}
$$

$$
\text { y-intercept = } 3
$$

## check in each equation

| $2 x+4 y=12$ | $x+y=2$ |
| :--- | :--- |
| $2(-2)+4(4)=12$ | $-2+4=2$ |
| $-4+16=12$ | $2=2$ |

$12=12$ $\qquad$ point of intersection appears to be ( $-2,4$ )

$(-2,4)$ is the point of intersection \{solution\} of the two lines \{equations\}

Which ordered pair of numbers is the solution of the system? $\left\{\begin{array}{l}2 x+3 y=12 \\ 2 x-y=4\end{array}\right.$


Which of the following graphs shows the solution of the system?
$\left\{\begin{aligned} x+y & =-4 \\ 2 x-2 y & =-8\end{aligned}\right.$


Get each équation in slope-intercept form, $\bar{y}=m x+b$ $m$ is the slope $b$ is the $y$-intercept

$$
\text { slope }=\frac{\text { rise }}{\text { run }}=\frac{\text { vertical change }}{\text { horizontal,changé }}
$$

$$
x+y=-4 \quad\{\text { first equation }\}
$$

$$
y=-x-4 \quad\{s u b t r a-c t e d x \text { from each side }\}
$$

slope $=-1\left\{\right.$ which is $\frac{-1}{1}$ in the form of $\left.\frac{\text { rise }}{\text { run }}\right\}$
$y$-intercept $=-4 \quad\{$ where the line crosses the $y$-axis $\}$ slope $=1 \quad\left\{\right.$ which is $\frac{1}{1}$ in the form of $\left.\frac{\text { rise }}{\text { run }}\right\}$
$y$-intercept $=4 \quad\{$ where the line crosses the $y$-axis \}

You and your friend are both knitting scarves for charity. You knit 8 rows each minute and already have knitted 10 rows. Your friend knits 5 rows each minute and has already knitted 19 rows. When will you both have knitted the same number of rows?

2.6 minutes

(H) 9.7 minutes

Let $x$ be the number of minutes and $y$ be the number of rows
You knit 8 rows per minute and already knitted 10 rows
$y=8 x+10 \quad\{8$ times the number of minutes $(x)$ plus the number of rows already $(y)\}$

Your friend knits 5 rows per minute and already knitted 19 rows
$y=5 x+19$ \{5 times the number of minutes $(x)$, plus the number of rows already $(y)\}$
A graphing calculator could be used to find the point of intersection.



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